

**UNIVERSITY OF CALIFORNIA, BERKELEY**  
**College of Engineering**  
**Department of Electrical Engineering and Computer Sciences**

EE 105: Microelectronic Devices and Circuits

Spring 2008

**MIDTERM EXAMINATION #2**

Time allotted: 80 minutes

**NAME:** \_\_\_\_\_  
(print) Last First Signature

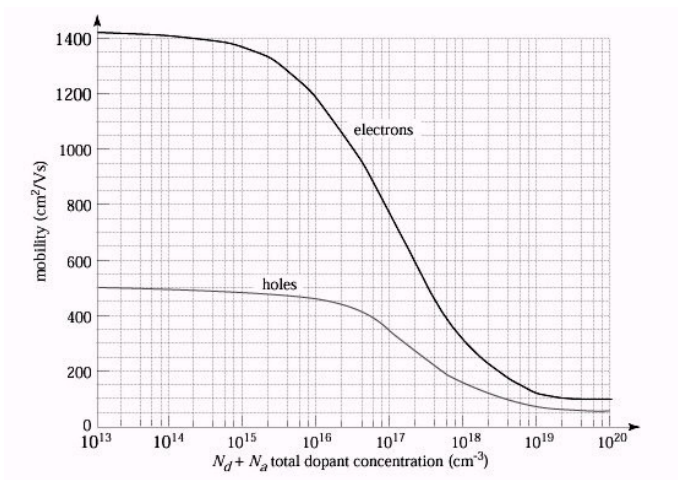
**STUDENT ID#:** \_\_\_\_\_

**INSTRUCTIONS:**

1. Use the values of physical constants provided below.
2. **SHOW YOUR WORK.** (Make your methods clear to the grader!)
3. Clearly mark (underline or box) your answers.
4. Specify the units on answers whenever appropriate.

<b>PHYSICAL CONSTANTS</b>	<b>PROPERTIES OF SILICON AT 300K</b>																
<table style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="text-align: left; padding: 2px;"><u>Description</u></th> <th style="text-align: center; padding: 2px;"><u>Symbol</u> <u>Value</u></th> </tr> </thead> <tbody> <tr> <td style="padding: 2px;">Electronic charge</td> <td style="text-align: center; padding: 2px;"><math>q</math> 1.6 <math>\cdot 10^{-19}</math> C</td> </tr> <tr> <td style="padding: 2px;">Boltzmann's constant</td> <td style="text-align: center; padding: 2px;"><math>k</math> 8.62 <math>\cdot 10^{-5}</math> eV/K</td> </tr> <tr> <td style="padding: 2px;">Thermal voltage at 300K</td> <td style="text-align: center; padding: 2px;"><math>V_T = kT/q</math> 0.026 V</td> </tr> </tbody> </table> <p style="padding: 5px;">Note that <math>V_T \ln(10) = 0.060</math> V at <math>T=300</math>K</p>	<u>Description</u>	<u>Symbol</u> <u>Value</u>	Electronic charge	$q$ 1.6 $\cdot 10^{-19}$ C	Boltzmann's constant	$k$ 8.62 $\cdot 10^{-5}$ eV/K	Thermal voltage at 300K	$V_T = kT/q$ 0.026 V	<table style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="text-align: left; padding: 2px;"><u>Description</u></th> <th style="text-align: center; padding: 2px;"><u>Symbol</u> <u>Value</u></th> </tr> </thead> <tbody> <tr> <td style="padding: 2px;">Band gap energy</td> <td style="text-align: center; padding: 2px;"><math>E_G</math> 1.12 eV</td> </tr> <tr> <td style="padding: 2px;">Intrinsic carrier concentration</td> <td style="text-align: center; padding: 2px;"><math>n_i</math> <math>10^{10}</math> cm<sup>-3</sup></td> </tr> <tr> <td style="padding: 2px;">Dielectric permittivity</td> <td style="text-align: center; padding: 2px;"><math>\epsilon_{Si}</math> 1.0 <math>\cdot 10^{-12}</math> F/cm</td> </tr> </tbody> </table>	<u>Description</u>	<u>Symbol</u> <u>Value</u>	Band gap energy	$E_G$ 1.12 eV	Intrinsic carrier concentration	$n_i$ $10^{10}$ cm <sup>-3</sup>	Dielectric permittivity	$\epsilon_{Si}$ 1.0 $\cdot 10^{-12}$ F/cm
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**Electron and Hole Mobilities in Silicon at 300K**



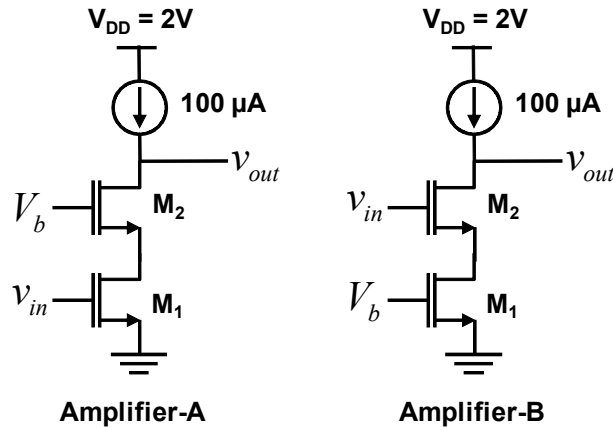
SCORE:

1		/	20
2		/	25
3		/	15
4		/	20
<b>Total:</b>		/	<b>80</b>

**Problem 1 [20 points]: MOS Amplifiers**

1) For this problem, use the following parameters for all NMOS transistors:

$V_{TH} = 0.4 \text{ V}$ ,  $\mu_n C_{ox} = 200 \text{ } \mu\text{A}/\text{V}^2$ ,  $\lambda = 0.1 \text{ V}^{-1}$ ,  $(W/L)_1 = (W/L)_2 = 10$ . The current source is ideal.



a) Find the small signal parameters for  $M_1$  and  $M_2$  ( $g_m$ ,  $r_o$ ). [4pts]

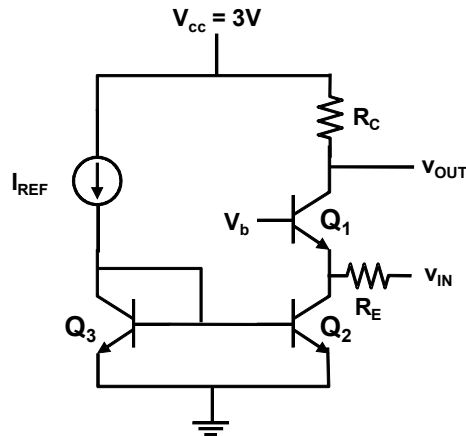
b) What is the topology of “Amplifier-A” (i.e., common source, common base, etc)? [2pts]

c) Find the voltage gain, input and output resistance of Amplifier-A. Show both the expressions and the numerical values. You can make approximations in your expression as long as they are within 10% accuracy. [6pts]

- d)** What is the topology of “Amplifier-B” (i.e., common source, common base, etc)? [2pts]
- e)** Find the voltage gain, input and output resistance of Amplifier-B. Show both the expressions and the numerical values. You can make approximations in your expression as long as they are within 10% accuracy. [6pts]

**Problem 2 [25 points]: BJT Circuits and Frequency Response**

- 2) Assume that  $V_{CC} = 3\text{ V}$ ,  $I_{REF} = 100\mu\text{A}$ ,  $I_S = 10^{-17}\text{ A}$ ,  $V_A = 50\text{ V}$ , and  $\beta = 100$  for all transistors.  $A_{E1} = A_{E2} = 10A_{E3}$ .  $R_C = 1\text{ k}\Omega$ , and  $R_E = 1\text{ k}\Omega$ . Assume  $C_{\mu} = 10\text{ fF}$ ,  $C_{\pi} = 100\text{ fF}$ , and  $C_{CS} = 20\text{ fF}$ .



- a) Identify the functions of  $Q_1$ ,  $Q_2$ , and  $Q_3$ . What is the function of this circuit? [3pts]
- b) Find the small-signal parameters of the main amplifier transistor ( $r_p, g_m, r_o$ ). [3pts]
- c) Find the expression and the value of the voltage gain. [4pts]

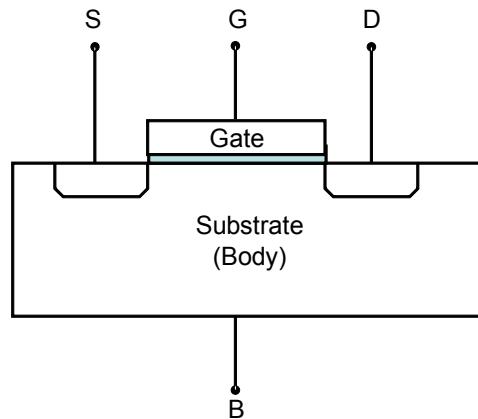
**d)** Show all parasitic capacitances of the BJTs in the circuit diagram above. Simplify the capacitances (e.g., combine all capacitances in parallel, remove capacitances that are shorted). Redraw the circuit diagram below with the simplified capacitances. [Hint: a constant DC voltage is AC ground]. [5pts]

**e)** Find the input and output poles of this circuits. What is the dominant pole? Find the 3-dB bandwidth of this circuit. [5pts].

- f) Construct the Bode plot of the transistor. Clearly mark the scale of both axes. The Bode plot should show both the low-frequency voltage gain as well as 3-dB bandwidth of the amplifier. [5pts]

**Problem 3 [15 points]: MOS Devices**

3) Below is the cross section of a PMOS transistor:

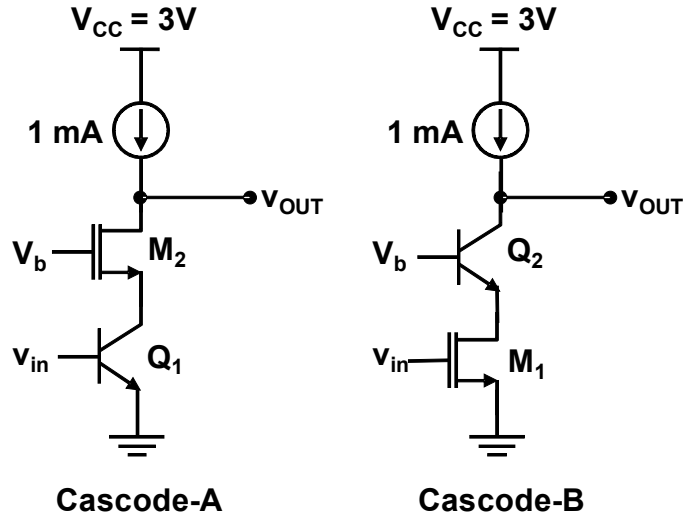


- a) What is the doping type (n, n+, p, or p+, where “+” means high doping concentration) of [3pts]
- i) Source:
  - ii) Drain:
  - iii) Substrate (body):
- b) Which carrier(s) are involved in current conduction? (i) electrons, (ii) holes, (iii) both electrons and holes. (choose one) [3pts]
- c) If the power supply voltage is 2V and ground is 0V, what bias voltage is usually connected to the body (substrate) of the transistor? Why? [3pts]
- d) Assume the threshold voltage of the PMOS is  $V_{TH} = -0.4V$ . If  $V_S = 2V$ ,  $V_D = 0V$ , find the gate voltages for which the PMOS is (i) cut-off, (ii) in between saturation and triode regions. [3pts]
- e) If a PMOS and an NMOS have exactly the same dimension (W, L, and oxide thickness), which transistor has higher  $g_m$ ? Why? (Assume both are long-channel devices) [3pts]



**Problem 4 [20 points]: Cascode Amplifiers**

4) Below is a cascode amplifier with *mixed* MOS and BJT transistors:



MOS transistor parameters:  $V_{TH} = 0.5V$ ,  $\mu_n C_{ox} = 200 \mu A/V^2$ ,  $\lambda = 0.1V^{-1}$ ,  $(W/L)_1 = (W/L)_2 = 10$   
 BJT transistor parameters:  $I_S = 10^{-17} A$ ,  $V_A = 10 V$ , and  $\beta = 100$

a) Find the small-signal parameters of the MOS transistor ( $g_m, r_0$ ). [2pts]

b) Find the small-signal parameters of the BJT transistor ( $g_m, r_0, r_p$ ). [3pts]

**c)** From **a)** and **b)**, find the *relative* magnitudes of small-signal parameters: [3pts]

i)  $g_{m,BJT} / g_{m,MOS}$

ii)  $r_{0,BJT} / r_{0,MOS}$

iii)  $r_{p,BJT} / r_{0,BJT}$

**d)** Derive the expressions of the output resistances for both cascade amplifiers shown above. You can drop small terms that are less than 10% of the dominant terms. Using the ratios you obtained in **c)**, determine which cascode amplifier (Cascode-A or Cascode-B) has higher output resistance. [6pts]

- e) Derive the expressions of the voltage gain for both cascade amplifiers shown above. You can drop small terms that are less than 10% of the dominant terms. Using the ratios you obtained in c), determine which cascode amplifier (Cascode-A or Cascode-B) has higher voltage gain. [6pts]