

Spring 2005

UNIVERSITY OF CALIFORNIA
College of Engineering
Department of Electrical Engineering and Computer Sciences
EECS130 Midterm I

Last Name _____ First Name **SOLUTIONS**

Instructions:

Print your name on the cover page CLEARLY now

Show major intermediate steps on exam pages to facilitate grading

Make sure your copy of the exam paper has 7 pages (including cover page)

Information that may be useful

$$q = 1.6 \times 10^{-19} \text{ coulombs}$$

$$\text{Boltzmann constant } k = 8.62 \times 10^{-5} \text{ eV/ K}$$

$$n_i \text{ of Si} = 10^{10} \text{ cm}^{-3} \text{ at 300K}$$

Problem 1 (14 points) _____

Problem 2 (28 points) _____

Problem 3 (17 points) _____

Problem 4 (41 points) _____

TOTAL (100 points) _____

Problem 1 (14 points)

A donor-doped silicon sample at 300K has resistivity of $0.1 \Omega\text{-cm}$.

a) What is the doping density? (3 points)

$$\text{Given } \rho = 0.1 \Omega\text{-cm}$$

From Resistivity versus Doping chart,

$$N_D = 7 \times 10^{16} \text{ cm}^{-3}$$

b) What is the hole concentration? (2 points)

$$P = \frac{n_i^2}{n} = \frac{10^{20}}{7 \times 10^{16}}$$

$$= 1.42 \times 10^3 \text{ cm}^{-3}$$

$$n_i = 1.42 \times 10^{10} \text{ cm}^{-3} @ 300K$$

c) What is electron diffusion constant? (4 points)

$$D_n = \frac{kT}{q} \mu_n$$

$$\mu_n = 830 \text{ cm}^2/\text{V-s}$$

$$D_n = \frac{kT}{q} \mu_n = \frac{8.62 \times 10^{-5} \text{ eV}}{e} \times 300 \times \frac{830 \text{ cm}^2}{\text{V-s}} = 21.46 \text{ cm}^2/\text{s}$$

Or read from the chart.

d) Now acceptor density, $N_A = 3 \times 10^{16} \text{ cm}^{-3}$ is added to above sample. What is conductivity of the sample? (5 points)

$$N_A = 3 \times 10^{16}, \quad N_D = 7 \times 10^{16}$$

$$N_A + N_D = 10^{17} \text{ cm}^{-3}$$

$$n = N_D - N_A = 4 \times 10^{16} \text{ cm}^{-3}$$

$$P = \frac{n_i^2}{n} = \frac{10^{20}}{4 \times 10^{16}} = 2.5 \times 10^3 \text{ cm}^{-3}$$

$$\sigma = q \mu_n n + \cancel{q \mu_p P} \xrightarrow{\text{small contribution}}$$

$$\boxed{\sigma \approx q \mu_n n}$$

$$\mu_n @ 10^{17} \text{ cm}^{-3} = 720 \text{ cm}^2/\text{V-s}$$

$$\sigma = 1.6 \times 10^{-19} \text{ C} \cdot \text{V}^{-1} \times 720 \frac{\text{cm}^2}{\text{V-s}} \times 4 \times 10^{16} \text{ cm}^{-3}$$

$$= 4.6 \frac{1}{\text{ohm-cm}}$$

$$\boxed{\sigma = 4.6 [\text{ohm-cm}]^{-1}}$$

Problem 2 (14×2=28 points)

Answer each with one or two sentences, or phrases or define with an equation. Unless otherwise specified answer the questions for Si at 300K. You may assume that commonly used parameters are given.

- a) What is the electron concentration given $N_A=N_D=5\times 10^{15} \text{ cm}^{-3}$?

$$n = n_i$$

- b) Is silicon a donor or an acceptor in GaAs? (Ga is group III and As is Group V).

both Acceptor and Donor (Si is IVth Group)

- c) What is the recombination rate, given n' ?

$$\frac{n'}{\tau} \quad \text{where } \tau \text{ is recombination time}$$

- d) Give an expression for Einstein relationship.

$$\frac{D}{\mu} = \frac{kT}{q^2}$$

- e) What is the "excess carrier concentration"?

$$n' \equiv n - n_0$$

or Difference between carrier concentration and the equilibrium value.

- f) What is wet lithography technology?

Use liquid to reduce the light wavelength in lithography process.

or Add water to the space between the lens and the wafer

or Use liquid to improve lithography resolution.

- g) What is 'end-point detection' in etching process?

Detecting the exposed substrate film after the removal of the desired film.

or A way to know when etching is done.

or Detection of completion of the (desired) etch process.

h) What type of CVD process is used to deposit oxide at the lowest temperature?

PECVD

i) What is 'sputtering'?

Depositing a film by kicking atoms of the film material out of a "target" with plasma (or ions).

j) Why is wet oxidation sometimes preferred over dry oxidation?

Wet oxidation is faster than dry oxidation.

Or Wet oxidation can be performed at lower temperature.

k) Give two reasons for 'thermal annealing' after ion-implantation even when the shallowest possible junction depth is desirable.

1. Damage removal
2. Dopant activation

l) Give two reasons why the industry switched from *Al* to *Cu* as interconnect material in advanced silicon technology.

1. Electromigration
2. Low contact resistance
3. Low RC delay
4. Faster circuits
5. better reliability

m) What is the depletion region approximation?

There is a region in PN junction where electron and hole concentrations are low.

Or mobile carriers are negligible in the depletion region.

Or $n \approx 0, p \approx 0$ in the depletion region.

n) What is a one-sided junction?

One side of the junction is heavily doped as compared to the other side.

Problem 3 (17 points)

Design a sequence of process steps by using the available process options from the given menu to go from Fig. 1 to Fig. 2.

Process Menu
Annealing
Gas Source doping
Wet etching
Deposition of oxide
Dry etching
Ion Implantation
Sputtering
Solid source diffusion
Lithography

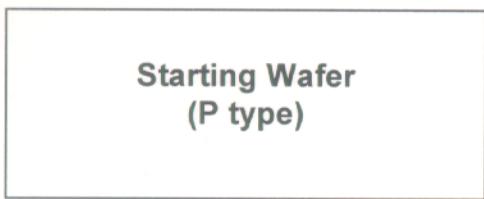


Fig. 1

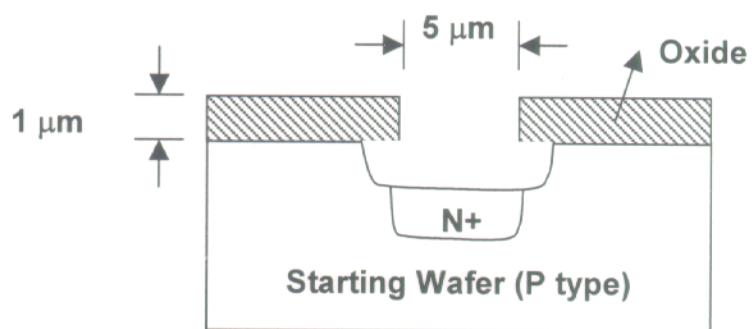


Fig. 2

OR

- Deposition of oxide
- Lithography
- Dry etching (For oxide)
- Wet etching (For substrate)
- Ion Implantation
- (Annealing) ↗ optional

- OR
- Deposition of oxide
 - lithography
 - Dry etching (For oxide)
 - Ion Implantation
 - wet etching (For substrate)
 - (Annealing) ↗ optional

OR

- Deposition of oxide
- lithography
- Dry etching

- Ion Implantation
- (Annealing) ↗ optional
- Wet etching

PROBLEM #4

1.

$$\text{Eqn. 1: } n_i = \sqrt{N_c N_V} e^{-E_g/2kT}$$

$$\text{Eqn. 2: } N_c = 2 \left[\frac{2\pi m_n kT}{h^2} \right]^{3/2}$$

$$\text{Eqn. 3: } N_V = 2 \left[\frac{2\pi m_p kT}{h^2} \right]^{3/2}$$

$$\text{Eqn. 4: } N_c e^{-(E_c - E_f)/kT} = n$$

Affected Parameter	n_i	n	p	$E_c - E_f$
Changing Parameter				
$E_g \uparrow$	From Eqn. 1 $w/E_g \uparrow \Rightarrow n_i \downarrow$ \downarrow	For $N_D = 10^{16} \text{ cm}^{-3}$ (N-type) n -stays the same \rightarrow	$p = \frac{n_i^2}{n}$ $w/n_i \downarrow \Rightarrow p \downarrow$ \downarrow	From Eqn. 4 n -stays same N_c -stays same No change in $E_c - E_f$ \rightarrow
$m_n \uparrow$	from Eqn. 2 $w/m_n \uparrow \Rightarrow N_c \uparrow$ $n_i \uparrow$ (Eqn. 1) \uparrow	n -No change \rightarrow	$w/n_i \uparrow \Rightarrow p \uparrow$ \uparrow	n -No change $N_c \uparrow$ from Eqn. 4 \uparrow
$m_p \uparrow$	from Eqn. 3 $w/m_p \uparrow \Rightarrow N_V \uparrow$ $n_i \uparrow$ (Eqn. 1) \uparrow	n -No change \rightarrow	$w/n_i \uparrow \Rightarrow p \uparrow$ \uparrow	n -No change N_c -No change from Eqn. 4 \rightarrow
$N_D \uparrow$	No effect on n_i \rightarrow	Sample more heavily doped now. \uparrow	$p = \frac{n_i^2}{n}$ $n \uparrow \Rightarrow p \downarrow$ \downarrow	from Eqn. 4 \downarrow (E_f closer to E_c)
$N_A \uparrow$	No effect on n_i \rightarrow	$n = N_D - N_A$ (Compensated) \downarrow	$p = \frac{n_i^2}{n}$ $n \uparrow \Rightarrow p \uparrow$ \uparrow	from Eqn. 4 \uparrow (E_f moves away from E_c)
$T \uparrow$ (assume N_c and N_V remain constant)	From Eqn. 1 no change $n_i \uparrow$ \uparrow	upto this temp. (400K) n does not change \rightarrow	$p = \frac{n_i^2}{n}$ $n_i \uparrow \Rightarrow p \uparrow$ \uparrow	from Eqn. 4 $e^{-(E_c - E_f)/kT} = \text{const}$ ($N_c, n = \text{No change}$) $T \uparrow \Rightarrow (E_c - E_f) \uparrow$ \uparrow

Added condition

T goes up to 400K

$$\text{Eqn. 5: } \mu = \frac{qE}{m}$$

$$\mu \leftarrow \begin{array}{l} \text{Impurity scattering component} \\ \text{Lattice scattering component} \end{array} \propto \frac{I^{3/2}}{N_A + N_D}$$

$$\text{Eqn. 6: } D = \frac{KT}{q} \mu$$

$$\text{Eqn. 7: } \phi_{bi} = \frac{kT}{q} \ln\left(\frac{N_A N_D}{n_i^2}\right)$$

PROBLEM # 4

2:

$$\text{Eqn. 8: } W_{dep} = \sqrt{\frac{2\epsilon_{si} (\phi_{bi} + V) \times (N_A + N_D)}{q(N_A, N_D)}}$$

Affected Parameter	μ_n	D_p	ϕ_{bi} of PN junction with $N_A = 10^{18} \text{ cm}^{-3}$	W_{dep}
Changing Parameter				
$E_g \uparrow$	$\mu_{\text{lattice and impurity}}: \text{No change.} \rightarrow$	from eqn. 6 $D_p = \text{No change} \rightarrow$	from eqn. 7: $n_i \downarrow \Rightarrow \phi_{bi} \uparrow$	$\phi_{bi} \uparrow \Rightarrow W_{dep} \uparrow$ (Eqn. 8)
$m_n \uparrow$	$m_n \uparrow \Rightarrow \mu_n \downarrow$ (eqn. 5)	$\mu_p - \text{remains same}$ $D_p = \text{No change} \rightarrow$	$n_i \uparrow \Rightarrow \phi_{bi} \downarrow$	$\phi_{bi} \downarrow \Rightarrow W_{dep} \downarrow$
$m_p \uparrow$	$m_p \uparrow \Rightarrow \text{No change on } \mu_n \rightarrow$	$m_p \uparrow \Rightarrow \mu_p \uparrow$ $\Rightarrow D_p \downarrow$	$n_i \uparrow \Rightarrow \phi_{bi} \downarrow$	$\phi_{bi} \downarrow \Rightarrow W_{dep} \downarrow$
$N_D \uparrow$	More Impurity scattering $\mu_n \downarrow$	$\mu_p \text{ also goes down}$ $\mu_p \downarrow \Rightarrow D_p \downarrow$	$N_D \uparrow \Rightarrow \phi_{bi} \uparrow$	\times
$N_A \uparrow$	More Impurity scattering $\mu_n \downarrow$	$\mu_p \downarrow \Rightarrow D_p \downarrow$	\times	\times
$T \uparrow$ (assume N_c and N_v remain constant)	\times	\times	\times	\times